

# A Second-Order Approach to Learning with Instance-Dependent Label Noise

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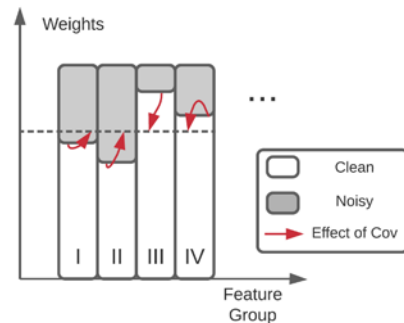
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## Code

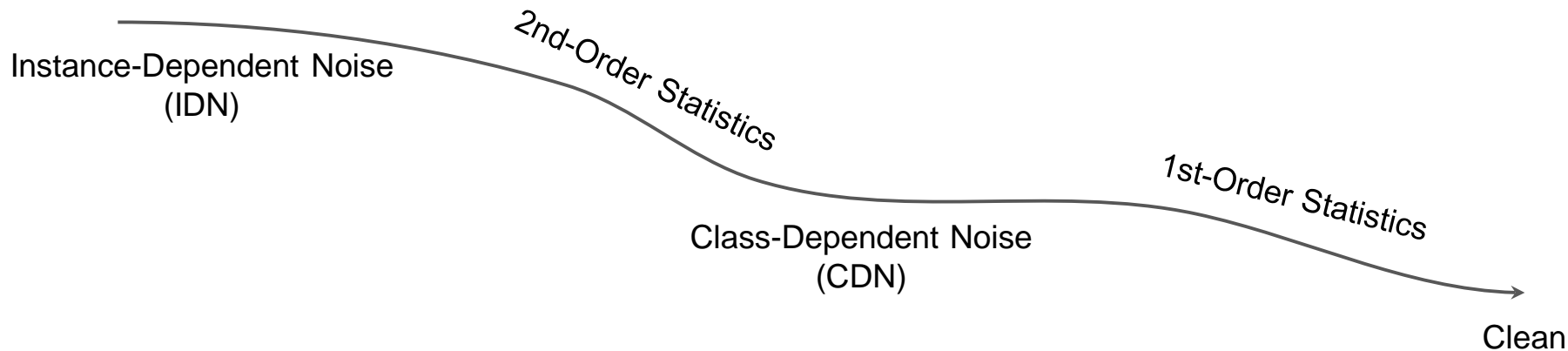


REsponsible & Accountable Learning (REAL)  
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<https://github.com/UCSC-REAL>



# Covariance-Assisted Learning (CAL)



[1] N. Natarajan, et al. "Learning with noisy labels." *NeurIPS'13*.

[2] T. Liu & D. Tao. "Classification with noisy labels by importance reweighting." *TPAMI'15*.

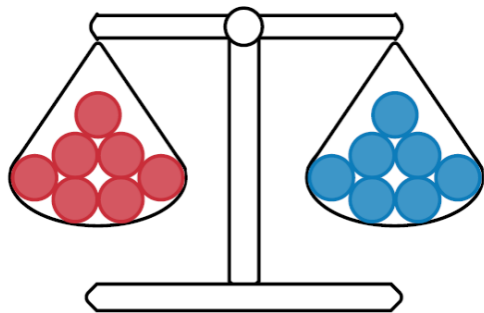
[3] G. Patrini, et al. "Making deep neural networks robust to label noise: A loss correction approach." *CVPR'17*.

# Motivation

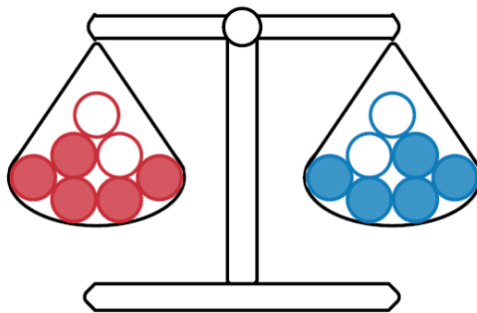
- Two groups (not label classes) of instances with equal size

- Empirical Risk Minimization (ERM) of instances from two groups:

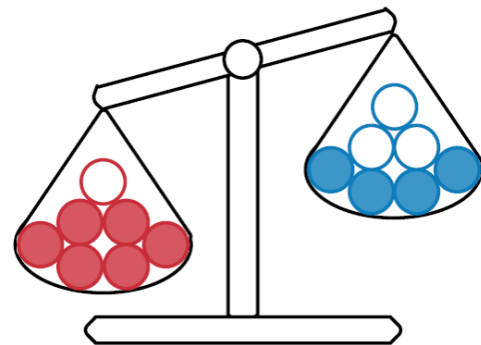
$$\text{Loss} = \sum_{i \in \text{Group-1}} \text{Loss}_i + \sum_{j \in \text{Group-2}} \text{Loss}_j$$



Clean



Class-dependent label noise



Instance (group)-dependent noise

**Clean:** no noise

- equal #instances contribute to clean loss
- equal weights in ERM

**CDN:** equal noise

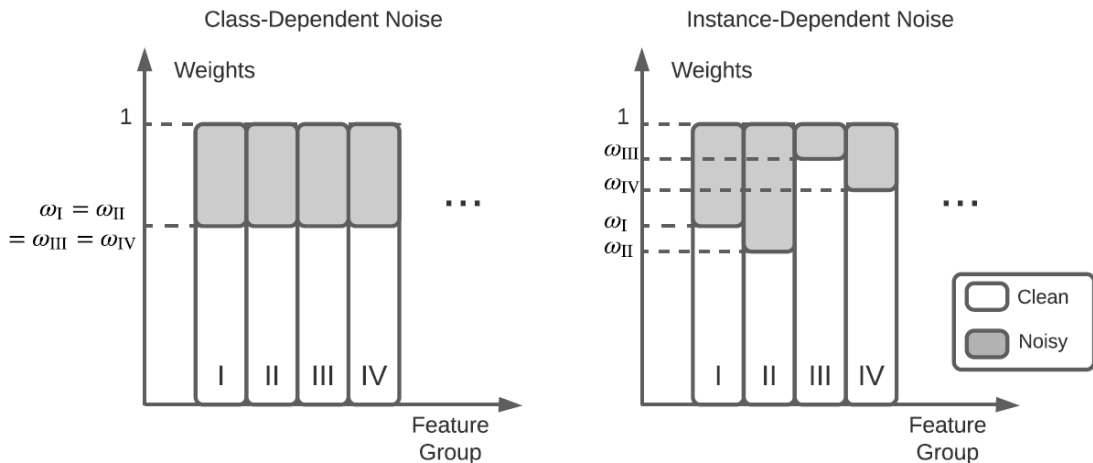
- equal #instances contribute to clean loss
- equal weights in ERM

**IDN:** Group 2: larger noise

- less #instances contribute to clean loss
- smaller weights in ERM

# Insufficiency of First-Order Statistics

- **Lemma:** Peer Loss [4] is invariant to CDN:  $\text{NoisyPL} = \omega \cdot \text{CleanPL}$



## Summary:

- ➔ IDN causes weights imbalances
- ➔ **CDN:**
  - Only one unknown constant  $\omega$ .
  - Equal for all features.
- ➔ **IDN:**
  - Multiple unknown constants  $\omega_g$ .
  - **Down-weight high-noise features** (Section 3.3 in our paper).

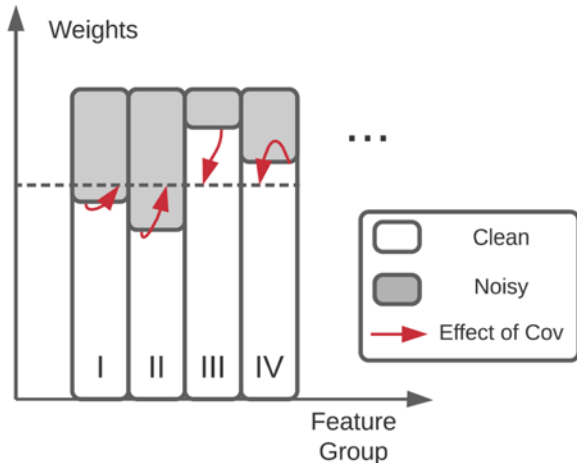
# Covariance-Assisted Learning (CAL)

- Our method:

- Peer Loss + Covariance (requires constructing **Bayes optimal dataset** for estimating  $\mathcal{T}$ ):

$$\ell_{\text{CAL}}(f(x_n), \tilde{y}_n) = \ell_{\text{PL}}(f(x_n), \tilde{y}_n) - \text{Cov}(\text{Noise Trans. } \mathcal{T}, \text{Model Pred.})$$

✦ **Challenging!**  
(Details in the next slide)



## Summary:

- ➔ CAL balances weights of each feature
  - High-noise (Group I, Group II): improve weights
  - Low-noise (Group III, Group IV): reduce weights



- ➔ Theorem 3 (in our paper):

With perfect covariance estimates, **CAL is robust to IDN**

# Bayes Optimal Labels

## Algorithm (Sketch)

1. Construct  $\hat{D}$  (unbiased estimate of  $D^* \sim \mathcal{D}^*$ ) with sample sieve [5]
2. Estimate (unbiased)  $\hat{T}$  with  $\hat{D}$  (complexity  $O(\text{SampleSize})$ )
3. [Train DNN] Implement CAL in SGD (each point  $O(1)$  complexity)

✦ Rely on **Bayes optimal** labels

- Unique
- Tractable

## Example:

Type	Prob. Each Class	
Clean	0.9	0.1
Noisy	0.6	0.4
<b>Bayes opt.</b>	1.0	0.0

## Use **CORES** [5]:

A theoretically guaranteed sample sieve to find the Bayes optimal labels!

# Experiment

Table: Comparison of test accuracies (%) using different methods.

Method	<i>Inst. CIFAR10</i>			<i>Inst. CIFAR100</i>		
	$\eta = 0.2$	$\eta = 0.4$	$\eta = 0.6$	$\eta = 0.2$	$\eta = 0.4$	$\eta = 0.6$
CE (Standard)	85.45 $\pm$ 0.57	76.23 $\pm$ 1.54	59.75 $\pm$ 1.30	57.79 $\pm$ 1.25	41.15 $\pm$ 0.83	25.68 $\pm$ 1.55
Forward $T$ [2]	87.22 $\pm$ 1.60	79.37 $\pm$ 2.72	66.56 $\pm$ 4.90	58.19 $\pm$ 1.37	42.80 $\pm$ 1.01	27.91 $\pm$ 3.35
T-Revision [3]	90.04 $\pm$ 0.46	84.11 $\pm$ 2.47	72.18 $\pm$ 2.47	58.00 $\pm$ 0.36	43.83 $\pm$ 8.42	36.07 $\pm$ 9.73
Peer Loss [4]	89.12 $\pm$ 0.76	83.26 $\pm$ 0.42	74.53 $\pm$ 1.22	61.16 $\pm$ 0.64	47.23 $\pm$ 1.23	31.71 $\pm$ 2.06
CORES <sup>2</sup> [5]	91.14 $\pm$ 0.46	83.67 $\pm$ 1.29	77.68 $\pm$ 2.24	66.47 $\pm$ 0.45	58.99 $\pm$ 1.49	38.55 $\pm$ 3.25
CAL	<b>92.01<math>\pm</math>0.75</b>	<b>84.96<math>\pm</math>1.25</b>	<b>79.82<math>\pm</math>2.56</b>	<b>69.11<math>\pm</math>0.46</b>	<b>63.17<math>\pm</math>1.40</b>	<b>43.58<math>\pm</math>3.30</b>

Thank you !